

**Extensions to the Dirichlet distribution  
for data on the simplex  
and  
extensions to the Liouville distribution  
for data on the positive orthant**

by

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